Property Determinations of Open Clusters using Hierarchical Bayesian Modelling and Neural Networks

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**Abstract:**

**Context:** Open clusters are very useful for age and metallicity estimations, which makes that excellent for tracing the evolution of galaxies. Current methods of estimating open cluster properties are time consuming and heavily rely on literature values. We put forward that a more efficient method is by using a framework consisting a neural network inside an HBM.   
**Aims:** To determine accurate properties of open clusters, using a neural network to convert fundamentals and observables, which can be used by a hierarchical Bayesian model to simultaneously constrain the fundamental variables and give population wide mean values of these properties.   
**Methods:** We trained a deep feedforward neural network to convert fundamentals: age, mass, [Fe/H], initial helium and mixing length to observables: effective temperature, stellar radius and Δν using a grid of stellar evolution tracks calculated using MESA (B. Paxton et al. (2010) [MESA]). This was then incorporated into an HBM and property estimations were made using this framework given suitable priors on the fundamentals and observational data for different clusters, taken from the literature.   
Results:  
Conclusion:

Estimated Word Count:   
Key words: neural network, HBM, Bayesian, M67

Contents:

Nomenclature:

**Introduction:**  
Open clusters are one of the most important types of objects when it comes tracing the evolutionary history of our galaxy, which is still very much an open topic of research as making accurate property determinations can be quite challenging but is crucial to figuring out the mechanisms behind galactic evolution. Open clusters are loosely gravitationally bound groups of typically a few hundred coeval stars, meaning all the stars formed at approximately the same time in a relatively small region of a galaxy where there was a particular chemical composition. The result of this being that open cluster members can be treated as having the same age and [Fe/H] (hereafter metallicity). This feature is hugely beneficial for property determinations over single star measurements as by measuring open cluster members the mean age and metallicity of these effectively converges to the true values (see \cite{Hippel\_2005} and \cite{salaris\_2004} for more details). The most common method of doing this is by isochrone fitting, where an isochrone is a plot on a Herzsprung-Russell which describes stars of the same age, and typically also keeps the chemical composition constant. Isochrone fitting requires sampling ages and metallicities and converting those fundamentals parameters to observables (effective temperature, luminosity etc.) such that they can be compared to the observed data for the open cluster. Depending on the method the isochrones are evaluated to determine how well each isochrone fits and the best isochrone’s age and metallicity are taken to be true for the cluster. However, certain choices for the method of sampling and parameter conversion tool, can cause the fitting process to be incredibly time consuming. There are a variety of sampling methods from fitting by-eye \citep{brandt \_2015} to automated fitting processes using software \citep(perren\_2015) and Bayesian analysis (\cite{hills\_2015}, \cite{jeffery\_2016}, \cite{jørgensen\_2005}). Which compounds upon the time for the conversion process from fundamentals to observables which in most studies to date has been done using stellar evolution models to generate the isochrones via frameworks like MESA (\cite{ball\_2017}, \cite{ball\_2018}, \cite{MESA}) and DSED (\cite{jeffery\_2016}, \cite{DSED}). These require generating a stellar evolutionary track for each sampled age and metallicity which can take hours per track generated, although some studies (see \cite{jørgensen\_2005}) skirt this by using a pre-existing set of tracks and interpolating between them but raises different problems. There are other open cluster dating methods like detached eclipsing binaries (\cite{brewer\_2016} and \cite{bavarsad\_2016}) and white dwarf cooling (\cite{kalirai\_2001}, \cite{bedin\_2015}) but these outside the scope of this study.

The purpose of this study is to improve upon the isochrone fitting methods stated above by avoiding lengthy parameter conversion and track interpolation by training a neural network on MESA tracks to convert fundamental to observable parameters (SEE NEURAL NETWORK SECTION FOR MORE DETAILS). The sampling is to be done using a hierarchical Bayesian model (HBM) where literature values inform the sampling such that minimal time is wasted sampling in parameter space unlikely to yield the true values. This method should allow for sampling of open clusters to be done much faster with the added benefit that the HBM allows for simultaneous constraint of a large number of variables and is able to estimate the spread of those variables, which haven’t been measured before for open clusters (SEE THE HBM SECTION FOR FURTHER DETAILS).

**Target selection and data collection:**  
We selected 6 open clusters (NGC 2682 also known as M67, NGC 6791, NGC 6819, Ruprecht 147, NGC 752, NGC 188) which have a large range of ages and metallicities that have been relatively well studied, see Table 1 for details on the results of previous studies.

To select stars to study from these open clusters we began by finding membership studies (calculations of the probability that a star belongs to a particular open cluster), from which we chose the membership study of M67 done by \cite{gao\_2018} and for the other 5 clusters we used the work of \cite{cantat-gaudin\_2018}.

What follows are the steps and measures used to discard stars and gather data to calculate luminosities.   
- These 2 membership papers contained GAIA DR2 IDs, which allowed us to query GAIA DR2 (\cite{GAIA\_mission}, \cite{GAIA\_DR2}) to get GAIA G-band apparent magnitudes and distance estimates for the stars calculated by \cite{bailer-jones\_2018}. We then discarded stars without G-band measurements.  
- Effective temperatures, Teff, are crucial for this study so we wanted to get accurate and consistent Teff measurements whenever possible. Some of the most accurate Teff determinations have been made using the infrared spectroscopy of the Apache Point Observatory Galactic Evolution Experiment (APOGEE) \citep{APOGEE}, which we queried through SDSS DR12. Unfortunately, APOGEE didn’t have effective temperatures for all the stars we were considering, so for the remaining stars we queried the SIMBAD database and discarded stars without a Teff from APOGEE or SIMBAD.   
- We then selected the greatest number of stars from the OCs that gave a mean membership uncertainty of 1%.   
- For stars that didn’t have APOGEE Teffs but multiple literature Teffs, we counted anomalies as stars whose Teffs differed from the median literature value by greater than 90k, which were removed. The Teff of these stars were then selected by the paper which provided the largest number of Teffs for that OC of the papers that provided Teffs for each star.   
- The absolute GAIA G-band magnitude was calculated as follows:

$ M\_G = m\_G + 5 - \log\_{10}(r) - A\_G $ eq.1

where r is the median of the distance estimates for the cluster and $A\_G$ is the line-of-sight extinction ignoring the effects of reddening, calculated by:

$ A\_G = R(G)E’ $ eq.2

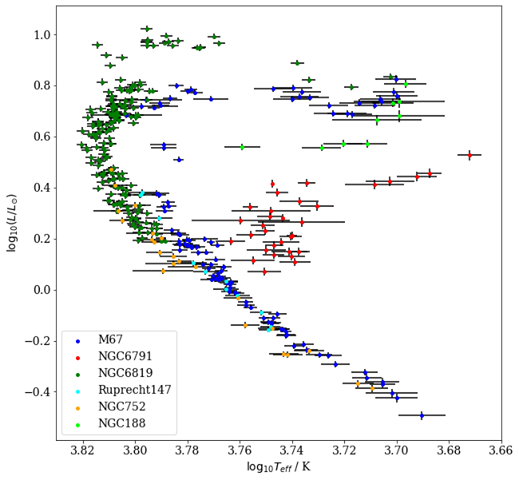
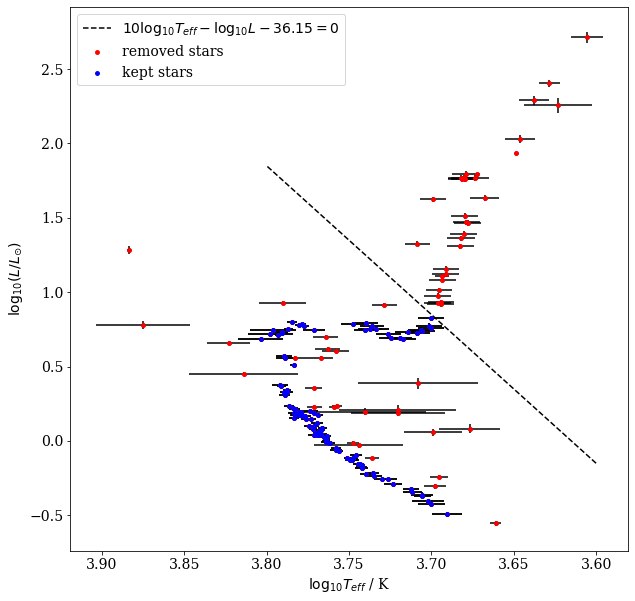
Where R(G) is the GAIA G-band extinction coefficient (2.294) determined by \cite{sanders\_2018} and E’ is the dust reddening taken from the best fit values in the bayestar2019 dust map. The GAIA G-band bolometric correction, $BC\_G$, was taken from a model dependent only Teff, by \cite{andrae\_2018}. From which we could get the bolometric magnitude:

$ M\_Bol = BC\_G + M\_G $ eq.3

And then we find the luminosity (in units of solar luminosities) by:

$ L = 10^{-0.4(M\_{Bol} - M\_{Bol, \odot})} $ eq.4

Where $M\_{Bol, \odot}$ is taken to be 4.75 \citep{MBOLSOL} We then plotted the HR-diagram and removed blue stragglers, binaries and other stars we thought might interfere with the HBM sampling. We removed the blue stragglers because they cannot be fitted to an isochrone as their properties evolve in an atypical way. Binaries are removed because their luminosities shift them far away from the line an isochrone would be fitted to and are removed like the other anomalies to assist with HBM sampling. A further cut that we made is removing the RGB stars which was done due to issues with neural network training (the reason for this is elaborated on further in the Neural Network section). The open clusters after star removal are shown in Figure 1. We also checked that after star removal the mean uncertainty per star for each cluster was still below 1% (which should be a table in the appendix)

   
**Figure 1**: HR diagram of the selected open clusters after removing blue stragglers, binaries, anomalies and the RGB (left). HR diagram of M67 with indication of removed stars (right).

As shown in Figure 1, NGC 752 and Ruprecht 147 don’t have sub giant branches with the selected stars, which is likely because they are the 2 youngest selected open clusters as shown in Table 1. These clusters should prove valuable in testing our methodology because without a sub giant branch fitting the isochrone to the clusters should be more difficult as the shape of the isochrone in this region is unclear.

**Table 1**: Literature search on the open clusters in this study. HQS – High Quality Spectroscopy, LQS – Low Quality Spectroscopy, Phot – Photometric

|  |  |  |  |
| --- | --- | --- | --- |
| cluster | Age estimation, Gyr | Metallicity, [Fe/H] | Helium abundance |
| NGC 2682 | 3.64 \citep{Bossini}  3.45 ± 1.13 \citep{Netopil \_2016} | 0.03 (HQS) \citep{Netopil \_2016} 0.00 (LQS) \citep{Netopil \_2016} -0.01 (Phot) \citep{Netopil \_2016} | 0.248 \cite{viani\_2017} |
| NGC 6791 | 8.45 \citep{Bossini}  7.00 ± 2.46 \citep{Netopil \_2016}  8.2 ± 0.3 \cite{ mckeever\_2019} | +0.42 (HQS) \citep{Netopil \_2016} +0.35 (LQS) \citep{Netopil \_2016} +0.44 (Phot) \citep{Netopil \_2016} | 0.297 ± 0.003 \cite{ mckeever\_2019}  0.30 ± 0.01 \cite{brogaard\_2012} NOT CALCULATED |
| NGC 6819 | 2.00 \citep{Bossini}  2.11 ± 0.44 \citep{Netopil \_2016}  2.5 \citep{balona\_2013}  2.25 ± 0.20 \citep{bedin\_2015} | +0.09 (HQS) \citep{Netopil \_2016}  -0.04 (LQS) \citep{Netopil \_2016}  +0.03 (Phot) \citep{Netopil \_2016} | 0.28 \cite{miglio\_2011} NOT CALCULATED |
| Ruprecht 147 | 2.5 ± 0.25 \citep{curtis\_2013}  3 \citep{curtis\_2013}  3.25 \citep{curtis\_2013} | +0.08 \citep{bragaglia\_2018} |  |
| NGC 752 | 1.48 \citep{Bossini}  1.69 ± 0.66 \citep{Netopil \_2016} | -0.03 (HQS) \citep{Netopil \_2016}  -0.09 (LQS) \citep{Netopil \_2016}  -0.04 (Phot) \citep{Netopil \_2016} | 0.26 |
| NGC 188 | 7.53 \citep{Bossini}  6.27 ± 2.30 \citep{Netopil \_2016}  5.78 ± 0.03 \citep{hills\_2015}  6.45 ± 0.04 \citep{hills\_2015} | +0.11 (HQS) \citep{Netopil \_2016}  -0.02 (LQS) \citep{Netopil \_2016}  -0.02 (Phot) \citep{Netopil \_2016}  +0.125 ± 0.003 \citep{hills\_2015}  −0.077 ± 0.003 \citep{hills\_2015} | 0.28 |

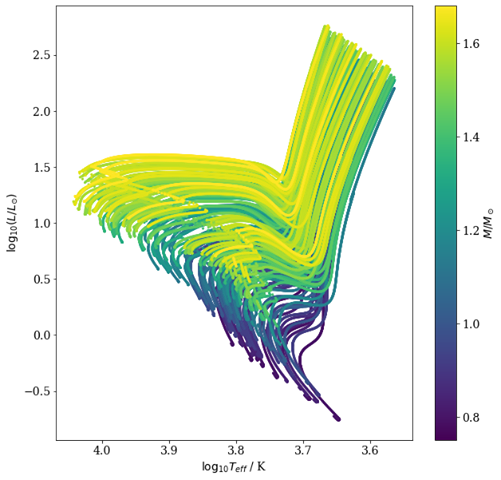
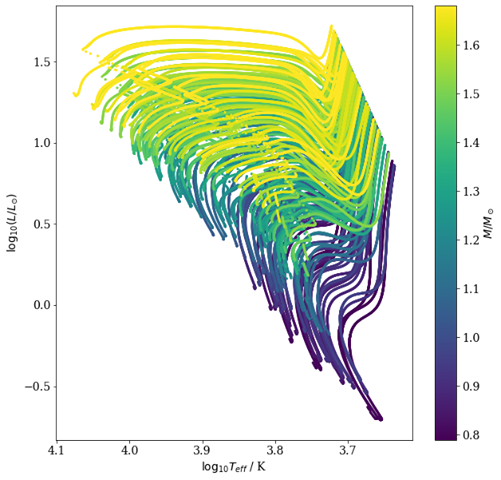
One of the features of the selected open clusters is that all the clusters are believed to be older than 1 Gyr. This is due to us wanting a large spread of stars along the isochrone to be informative for the HBM, but for clusters younger than 1 Gyr for stars to be sufficiently evolved must have high masses which exceed the mass range in the training grid shown in Table 2. It is also possible for younger clusters to be harder to observe due to large amounts of dust not having been used for star formation in the initial molecular cloud, which haven’t been dispersed through cosmic feedback processes which require post He-core burning stars to achieve.

**MESA stellar model**  
To generate a grid of stellar tracks to train a neural network on we chose to use Modules for Experiments in Stellar Astrophysics (MESA), which uses a specific model of stellar physics in order to evolve stars from some initial conditions and give their properties at a range of points across their lifetime (see \cite{MESA}, \cite{MESA2} and \cite{MESA3}). As our understanding of stellar evolution isn’t perfect, our stellar models aren’t perfect and as such there are simplifications must be made. An example is that the grid used in this study doesn’t account for stellar rotation which has knock on effects on temperature, luminosity and asteroseismic values (among others). However, studies like this assists in refining models by testing them.

**Table 2**: MESA tracks initial input parameter ranges

|  |  |  |
| --- | --- | --- |
| Input Parameter | range | increments |
| M / M\_{\odot} | 0.8 - 1.68 | 0.04 |
| [Fe/H]\_{init} | -0.8 - 0.6 | 0.2 |
| Y\_{init} | 0.24 - 0.32 | 0.02 |
| αMLT | 1.7 - 2.3 | 0.2 |

A more detailed description of the construction of the MESA grid can be found in \cite{li\_2018}, the only difference being in the initial input parameter ranges, shown here in Table 2.

   
Figure 2: HR diagram of 200 tracks from the training grid, with RGB (left) and without RGB (right). The reason why the right plot still has part of the lower RGB is because of neural network training and will be covered further in the neural network section.

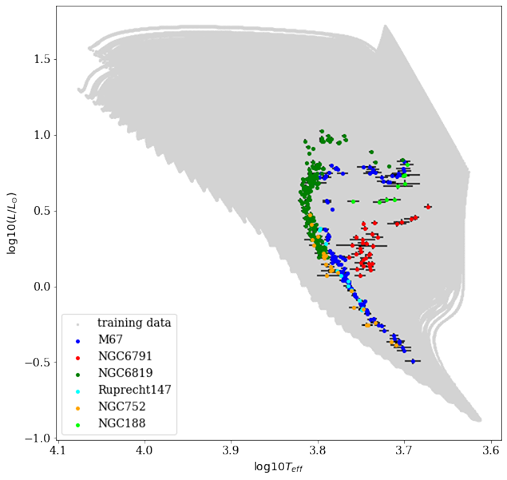


Figure 3: HR diagram of the selected open clusters, shown on top of the training data.

Figure 3 helps demonstrate that the selected open cluster’s true parameters can be found within the region covered by the training grid. Although it is possible that combinations of input parameters could still produce an isochrone that lies within the shaded region of Figure 3 but which is not covered by the input parameters of the grid, however parameter space covered by the training grid does cover metallicity estimates for the clusters from the literature shown in Table 1. As a result we feel confident that the training grid covers a large enough of age, metallicity and initial helium (initial helium never really goes above 0.32).

**Working with Neural Networks:  
 Machine Learning and Neural Networks:**  
Machine learning is the term used to describe a broad spectrum of statistical tools used to identify, reproduce or learn features of different kinds of trends. There are many different types of machine learning methods because not all methods are suitable for the limitless number of machine learning applications. For instance, in this study we will focussed on supervised machine learning where we present a trend that we want the neural network learn features of. This is in the form of the MESA grid where we have a set of input parameters we know map onto the output parameters as shown by the same trends in the MESA tracks generated from stellar fundamentals in Figure 2 having the same evolutionary shapes as the observational data shown in Figure 1. Within supervised machine learning there are the classification and regression subsets which both have a place in astronomy with classification methods using both supervised and unsupervised methods being useful for morphological classification (for a discussion of supervised methods see \cite{cheng\_2020}). Regression is quite different to this we want to reproduce the trends, as opposed to classification which learns the trend such that it can sort say images of galaxies into morphological groups. With regression methods, trends are learned and can be reproduced to predict points that the machine learning algorithm has never handled before but having learned the trends it knows how it should be handled.

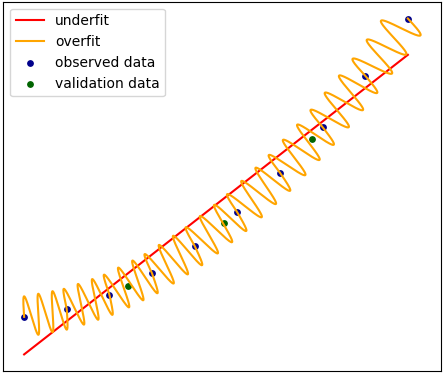
There have been a number of studies applying regression machine learning methods to best fitting stellar properties, like that done by \cite{hendriks\_2019} who used a deep neural network trained on a grid calculated using MESA to model asteroseismic properties and achieved consistent results to previous studies but using much less time to do so in a way that can be generalised to thousands of stars. These results are very similar to those we intend for this study but instead generalizable for many open clusters, which gives us confidence that at least our work with neural networks especially that with asteroseismic properties can be done successfully to at least the accuracy of previous works. There are also studies on just stellar fundamentals of main sequence stars using machine learning like that of \cite{bellinger\_2016} who use a random forest method that also uses MESA and again found that using machine learning they could achieve results consistent with previous work but using much less time. (add more examples of ML in literature?)

The machine learning of this study is focussed solely on using a deep, fully connected, feedforward neural network to construct what that is, I need to explain what an artificial neural network is. Artificial neural networks, commonly just referred to as neural networks are a set of machine learning methods which consist of a set of layers within which are some number of nodes also known as neurons hence neural network which have connections between subsequent layers. The simplest neural network requires an input layer consisting of a number nodes equal to the dimensionality of the input, similarly for an output layer and 1 layer in between the input and output known as a hidden layer which for this example may only have 1 node which would be connected to all the input and output nodes. The number of nodes and hidden layers and the way they are connected describes the “architecture” of the neural network. The significance of the size of the architecture is in that a larger architecture allows the neural network to reproduce more complex functions as nodes act almost like terms of a polynomial and so more nodes allows a higher order polynomial to be reproduced. Nodes are able to do this because for all non-input layer nodes, the value of each node is calculated using the values of the nodes in the preceding layer it is connected to using $\text{Output} = f(\sum\limits\_{i}^{N} W\_{i}I\_{i} + B)$. For simplicity this shall be for a fully connected neural network where each node in a non-input layer has connections to every node in the preceding layer. N is the number of nodes in the previous layer the current node is connected to, $ I\_{i} $ is the output of the ith node in the preceding layer, $ W\_{i} $ is the weight of the connection between the ith node of the preceding layer and current node, which describes the significance of the ith node relative to the other n-1 inputs to the current node and B is an additional input to the current node known as the “bias” which acts as a vertical translation variable. The function f which acts over the top of the weights, node inputs and bias is the activation function which in this case will be a non-linear activation function which works to penalize certain node outputs, typically negative node outputs are handled by non-linear activation functions by decreasing the weight of the connection of the current node to those in the succeeding layer which due to the reduction in the weight of the current means that it will be less informative to nodes of the next layer. Having explained somewhat of how a neural network functions I can now explicitly describe a deep, fully connected, feedforward, neural network as an artificial neural network, which uses deep learning meaning the neural network has more than one hidden layer, is fully connected where all nodes in a non-input layers have connections to all nodes of the preceding layer and it’s feedforward which is where the information flow from the input to the output.

Having covered the basic construction of a neural network the next stage is to explain how they are trained. Here I shall cover how to train neural networks using grid modelling: the grid being an array of possible input parameter values and the corresponding output parameters that you would expect/want the neural network to predict given the inputs, contains the data with which the neural network is able to learn and ideally improve to some desired accuracy by altering the weights and biases of its nodes to reproduce the trends in the data and enable it to make predictions of points not found in the training grid. The way in which the neural network makes decisions on how to improve its configuration by changing weights and biases is done on incremental steps of training called “epochs” and during an epoch the neural network will do backpropagation which allows it to determine the “complete error gradient vector”, $ \frac{\partial e}{\partial w} $ where $e$ is the error of the neural network known as the “loss function”, and $w$ is the set of neural network weights. The change to each weight can then be found from the negative of $ \frac{\partial e}{\partial w} $ from:

$ \Delta w = -\mu \frac{\partial e}{\partial w} $ eq.5 \citep{Bailer\_Jones\_2002}

Where $\mu$ describes the size of the weight update, typically referred to as the “learning rate”. A similar method of backpropagation is used to update the biases (for a more detailed description of backpropagation see \cite{NNbook}, \cite{Bailer\_Jones\_2002} and the references therein).

**Underfitting and Overfitting**  
By training for some number of epochs there are 2 extreme conditions where training the neural network won’t improve and may in fact become worse, both of which are related to the size of the neural network architecture (among other factors like regularization) and are demonstrated in Figure 4.  
  
Figure 4: Graphical showcase of neural network overfitting and underfitting.

For underfitting to occur, the neural network’s flexibility needs to be insufficient to fit the true trend of the data. This can be due to the architecture of the neural network being too small and so it doesn’t have enough nodes to reproduce the trends of the data. For example in Figure 4 a quadratic function is being fit by a linear polynomial which is obviously insufficient to properly fit the trend. At the other extreme is overfitting, where a neural network is given too much flexibility by having too large of an architecture, which is also characterized by the neural network losing it’s generalizability meaning the neural network is only trying to fit the points of the training grid and not predicting the overall trend of the data. Overfitting would go unnoticed if one was only concerned with the values of the loss function, as the loss would be very low because the grid points are the only points evaluated with the loss function but as shown by the green points in Figure 4 which follow the same trend as the observed data, the neural network does a terrible job at fitting to these points. Which is why when training having validation data is very useful. Validation data are points that are in the grid of training points which the neural network is not allowed to be trained on, which by finding loss for the validation points (the validation loss), it can be seen whether the neural network is overfitting if the validation loss is larger than the standard loss.

There are a few ways to minimize the effects of overfitting, first off is reducing the architecture to simply reduce the flexibility of the neural network, the second is increasing the number of training points which isn’t always feasible but does prevent the neural network fitting such complex functions when the points it needs to fit to are closer together. The third method is regularization which is a term added onto the loss function that penalizes large weights, thus reducing the size of the weights and consequently causing the neural network to not be able to generate complex models, preventing overfitting. It is possible to overregularize which would then move the neural network into the underfitting regime (a description of the other methods of minimizing overfitting can be found in \cite{prevent\_overfitting}).

**Training Stage 1: Main Sequence and RGB**

The initial process of training began by taking a subset of the training grid, such that we could figure out the approximate setup, (architecture and regularization wise) without having to waste time by training on the full grid that contains over 2.6 million points. The training stage 1 grid specs are described in Table 3 and whose HR diagram is shown in the left panel of Figure 2.

**Table 3**: Training Stage 1 setup. “-” shows that those parameter’s range is dependent on the input parameters.

|  |  |  |
| --- | --- | --- |
| Parameter | Form of data used by neural network | Training grid |
| Mass / M\_{\odot} | Log\_10{M} | 0.8 - 1.68 |
| Age / Gyr | Log\_10{Age} | 1 - 12 |
| [Fe/H] | Log\_10{[Fe/H]} | -0.2, 0, 0.2 |
| Y\_{init} | Log\_10{Y\_{init}} | 0.26, 0.28, 0.30 |
| α\_{MLT} | Log\_10{α\_{MLT}} | 1.7 - 2.3 |
| Luminosity / L\_{\odot} | Log\_10{R} | - |
| Teff / K | Log\_10{Teff/5000} | - |
| \Delta \nu / \mu Hz | Log\_10{\Delta \nu} | - |

To elaborate a few aspects of Table 3, neural networks like values they’re handling to have a small dynamical range close to 0. To combat this the neural network is given the log of all the parameters, which immediately solves that for everything except luminosity and the effective temperature, which we solve by dividing Teff by 5000 which reduces the log temperatures below 1 and to solve the luminosity dynamical range we instead used radius as one of the neural network outputs, calculated using the luminosity and effective temperature using the Stefan-Boltzmann law. This means that we were attempting to train a neural network to convert inputted age, mass, [Fe/H], initial helium and mixing length to Teff, radius and $\Delta \nu$, using roughly solar metallicity and helium on MS and RGB, stellar tracks.

38, 45 iso

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Initial conditions in a grid of:  
o Age = 1 to 12 Gyr

3859 tracks in total  
2659783 datapoints

Acknoledgements:  
Guy Davies for their guidance, Tanda Li for permitting us to use their MESA grid.

This work has made use of data from the European Space Agency (ESA) mission {\it Gaia} (\url{https://www.cosmos.esa.int/gaia}), processed by the {\it Gaia} Data Processing and Analysis Consortium (DPAC, \url{https://www.cosmos.esa.int/web/gaia/dpac/consortium}). Funding for the DPAC has been provided by national institutions, in particular the institutions participating in the {\it Gaia} Multilateral Agreement.

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| --- |
| Ted von Hippel: <https://arxiv.org/pdf/astro-ph/0509152.pdf> |
| M. Salaris et al. 2004: “The age of the oldest Open Clusters”  **Cluster age estimates in table 1**  <https://www-aanda-org.ezproxye.bham.ac.uk/articles/aa/full/2004/04/aah4736/aah4736.html>  The most reliable stellar ages are obtained for the star clusters belonging to the various populations, i.e., the globular clusters (GCs) in the halo, thick disk and bulge, and the open clusters (OCs) in the thin disk. The advantage of dating star clusters over individual stars – whose age determination relies entirely on the knowledge of individual metallicities, effective temperatures and gravities (or absolute magnitudes), which have to be fitted by the appropriate theoretical model – stems from the fact that star clusters are made of coeval objects, largely with the same initial chemical composition and located at the same distance, so that it is possible to use morphological parameters deduced from theoretical isochrones in order to derive their age. |
| Clio Bertelli Motta et al. 2016: “Observing the products of stellar evolution in the old open cluster M67 with APOGEE”  **Isochrone fitting M67**  <https://academic-oup-com.ezproxye.bham.ac.uk/mnras/article/466/2/2161/2687805> |
| D. Stello, et al. 2016: “THE K2 M67 STUDY: REVISITING OLD FRIENDS WITH K2 REVEALS OSCILLATING RED GIANTS IN THE OPEN CLUSTER M67”  **Isochrone fitting/grid based modelling**  <https://openresearch-repository.anu.edu.au/bitstream/1885/152166/2/01_Stello_THE_K2_M67_STUDY%253A_REVISITING_2016.pdf> |
| 1. F. Oliveira, et al. 2013: “Fitting isochrones to open cluster photometric data III. Estimating metallicities from UBV photometry”   **Isochrone fitting metallicity using the cross-entropy global optimization algorithm contains explanation**  “The metallicity is a critical parameter that affects the correct determination of fundamental characteristics of a stellar cluster and has important implications in Galactic and stellar evolution research. Fewer than 10% of the 2174 currently atalogued open clusters have their metallicity determined in the literature. In this work we present a method for estimating the metallicity of open clusters via non-subjective isochrone fitting using the cross-entropy global optimization algorithm applied to UBV photometric data.”  “Important questions that depend on metallicity, which is usually measured by the [Fe/H] ratio, are the determination of chemical abundance gradients (see Lépine et al. 2011, and references therein), determination of the rotational speed of the spiral pattern, and the co-rotation radius (Dias & Lépine 2005), and in the stellar context the empirical determination of the initial mass function, among many other fields of study.”  “Very schematically, the CE procedure provides a simple adaptive way of estimating the best-fit parameters. It involves an iterative procedure that follows the steps outlined below:  - random generation of the initial sample of fit parameters, respecting predefined criteria;  - selection of the best candidates based on calculated weighted likelihood values;  - generation of a random fit parameter sample derived from a new distribution based on the previous step;  - repeat until convergence or stopping criteria reached.” |
| Monteiro, H.; Dias, W. S.; Caetano, T. C. 2010: “Fitting isochrones to open cluster photometric data. A new global optimization tool”  **Isochrone fitting using cross-entropy global optimization algorithm ORIGINAL**  <https://ui.adsabs.harvard.edu/abs/2010A%26A...516A...2M/abstract> |
| H. Pöhnl and E. Paunzen 2010: “A statistical method to determine open cluster metallicities”  Method which differs from isochrone fitting as it doesn’t really on metallicity measurements.  “The study of open cluster metallicities helps to understand the local stellar formation and evolution throughout the Milky Way. Its metallicity gradient is an important tracer for the Galactic formation in a global sense. Because open clusters can be treated in a statistical way, the error of the cluster mean is minimized.”  <https://www-aanda-org.ezproxye.bham.ac.uk/articles/aa/pdf/2010/06/aa10855-08.pdf> |
| L. A. Balona, et al. (2013)  **Isochrone fitting**  “we determine the distance and age of NGC 6819 using several different methods. From isochrone fitting we find the age of the cluster to be about 2.5 Gyr” |
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| EMBEDDED CLUSTERS IN MOLECULAR CLOUDS  <https://pdfs>.semanticscholar.org/dd06/a8a9143f9e168dc2dc30c8cc3a15cc10fb40.pdf  galactic clusters form in giant molecular clouds (GMCs) and during their formation and earliest stages of evolution are completely embedded in molecular gas and dust, and thus obscured from view. Given the constraints imposed by traditional techniques of optical astronomy, direct observation and study of young embedded clusters had been extremely difficult, if not impossible. However, during the past two decades the development of infrared astronomy and, more recently, infrared array detectors, has dramatically improved this situation. |
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| @ARTICLE{prevent\_overfitting,  author = {{Ghojogh}, Benyamin and {Crowley}, Mark},  title = "{The Theory Behind Overfitting, Cross Validation, Regularization, Bagging, and Boosting: Tutorial}",  journal = {arXiv e-prints},  keywords = {Statistics - Machine Learning, Computer Science - Machine Learning},  year = 2019,  month = may,  eid = {arXiv:1905.12787},  pages = {arXiv:1905.12787},  archivePrefix = {arXiv},  eprint = {1905.12787},  primaryClass = {stat.ML},  adsurl = {https://ui.adsabs.harvard.edu/abs/2019arXiv190512787G},  adsnote = {Provided by the SAO/NASA Astrophysics Data System}  } |
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| @article{cantat-gaudin\_2018,  title={A Gaia DR2 view of the open cluster population in the Milky Way},  volume={618},  DOI={10.1051/0004-6361/201833476},  journal={Astronomy & Astrophysics},  author={Cantat-Gaudin, T. and Jordi, C. and Vallenari, A. and Bragaglia, A. and Balaguer-Núñez, L. and Soubiran, C. and Bossini, D. and Moitinho, A. and Castro-Ginard, A. and Krone-Martins, A. et al.},  year={2018},  pages={A93}} |
| @article{gao\_2018,  title={A Machine-learning-based Investigation of the Open Cluster M67},  volume={869},  DOI={10.3847/1538-4357/aae8dd},  number={1},  journal={The Astrophysical Journal},  author={Gao, Xinhua},  year={2018},  pages={9}} |
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CONCERNS:  
- introduction doesn’t discuss papers but more references methods that those papers use SEE NEURAL NETWORK SECTION FOR ALTERNATE METHOD OF WRITING ABOUT PAPERS  
- make sure to properly subscript Teff and A\_G etc.  
- in acknowledgements do we have to acknowledge keras and MESA, GAIA, pymc3 etc.?  
- acknowledge SDSS and everything  
- is it okay to copy paste this whole GAIA acknowledgement chunk of text?  
- consider writing neural networks as NN  
- **for project work 2 I suggest you make the Github repo public and submit the link to the repo.**

- limitations of using single G-band extinction coefficient  
- limit of Fe/H step fineness  
- harder to fit isochrone when you don’t have RGB stars  
- could cite Silva Aguirre et al. 2015 for an extended discussion on the various methods of dating stars